## **CH 223 Chapter Thirteen Concept Guide**

## 1. Writing Equilibrium Constant Expressions

## **Problem**

Write the equilibrium constant (K<sub>c</sub>) expressions for each of the following reactions:

(a) 
$$Cu(OH)_2(s) \rightleftharpoons Cu^{2+}(aq) + 2 OH-(aq)$$

(b) 
$$Cu(NH_3)_4^{2+}(aq) \rightleftharpoons Cu^{2+}(aq) + 4 NH_3(aq)$$

(c) 
$$CH_3CO_2H(aq) + H_2O(1) \rightleftharpoons CH_3CO_2-(aq) + H_3O+(aq)$$

## **Solution**

(a) 
$$K_c = [Cu^{2+}][OH^-]^2$$

(b) 
$$K_c = \frac{[Cu^{2+}][NH_3]^4}{[Cu(NH_3)_4^{2+}]}$$

(c) 
$$K_c = \frac{[CH_3CO_2^-][H_3O^+]}{[CH_3CO_2H]}$$

## 2. Writing Equilibrium Constant Expressions

## **Problem**

Write the equilibrium constant (K<sub>c</sub>) expressions for each of the following reactions:

(a) 
$$CO(g) + \frac{1}{2}O_2(g) \rightleftharpoons CO_2(g)$$

(b) 
$$C(s) + CO_2(g) \rightleftharpoons 2 CO(g)$$

$$(c) \operatorname{FeO}(s) + \operatorname{CO}(g) \rightleftharpoons \operatorname{Fe}(s) + \operatorname{CO}_2(g)$$

## **Solution**

(a) 
$$K_c = \frac{[CO_2]}{[CO][O_2]^{\frac{1}{2}}}$$

(b) 
$$K_c = \frac{[CO]^2}{[CO_2]}$$

(c) 
$$K_c = \frac{[CO_2]}{[CO]}$$

## 3. Writing Equilibrium Constant Expressions

## **Problem**

Write the equilibrium constant (K<sub>c</sub>) expressions for each of the following reactions:

(a) 
$$N_2(g) + O_2(g) \rightleftharpoons 2 NO(g)$$

(b) 
$$2 \text{ NO}(g) + \text{Br}_2(g) \rightleftharpoons 2 \text{ NOBr}(g)$$

(c) 
$$2 \text{ HF}(g) \rightleftharpoons H_2(g) + F_2(g)$$

### **Solution**

(a) 
$$K_c = \frac{[NO]^2}{[N_2][O_2]}$$

(b) 
$$K_c = \frac{[NOBr]^2}{[NO]^2[Br_2]}$$

(c) 
$$K_c = \frac{[H_2][F_2]}{[HF]^2}$$

## 4. Interpreting the Value of K

## Question

A student's task was to remove silver ion for an aqueous solution as completely as possible by causing it to form a precipitate. Given the following information, which would be the better method: to add a solution containing sulfate ion or one containing an equivalent amount of sulfide ion?

$$Ag_2SO_4(s) \rightleftharpoons 2 Ag^+ + SO_4^{2-} \quad K = 1.5 \times 10^{-5}$$

$$Ag_2S(s) \rightleftharpoons 2Ag^+ + S^{2-} K = 7.1 \times 10^{-50}$$

#### **Solution**

The precipitates formed would be silver sulfate and silver sulfide upon addition of sulfate ion or sulfide ion, respectively. Comparison of the equilibria that would result after precipitate formation using the two K values shows that the sulfide would leave a far lower concentration of Ag<sup>+</sup> in solution after the precipitation reaction went to completion. Thus, the student should choose the silver and sulfide reaction:

$$Ag_2S(s) \rightleftharpoons 2Ag^+ + S^{2-}$$

## 5. Manipulation of Equilibrium Expressions

## Question

Consider the following equilibria involving SO<sub>2</sub>(g) and their corresponding equilibrium constants.

(1) 
$$SO_2(g) + \frac{1}{2}O_2(g) \rightleftharpoons SO_3(g)$$
  $K_1$ 

(2) 
$$2 SO_3(g) \rightleftharpoons 2 SO_2(g) + O_2(g)$$
  $K_2$ 

Which of the following expressions relates  $K_1$  to  $K_2$ ?

(a) 
$$K_2 = K_{1^2}$$

(b) 
$$K_2^2 = K_1$$

(c) 
$$K_2 = \frac{1}{K_1}$$
  
(d)  $K_2 = \frac{1}{{K_1}^2}$ 

#### **Solution**

Reaction 2 is the inverse of reaction 1, and squared. Thus, (d) is the correct answer.  $K_2$  is related to  $K_1$  by:

$$K_2 = \frac{1}{K_1^2}$$

## 6. Writing Equilibrium Constant Expressions

## **Problem**

Calculate K for the reaction

$$SnO_2(s) + 2 CO(g) \rightleftharpoons Sn(s) + 2 CO_2(g)$$

given that:

$$SnO_2(s) + 2 H_2(g) \rightleftharpoons Sn(s) + 2 H_2O(g)$$
 K = 8.12

$$H_2(g) + CO_2(g) \rightleftharpoons CO(g) + H_2O(g)$$
  $K = 0.771$ 

## **Solution**

In general, when two or more equations are added to produce a net equation, the equilibrium constant for the net equation is the product of the equilibrium constants for the added equations. In this case, we need to reverse and double the second reaction to add to the first reaction.

$$\operatorname{SnO}_2(s) + 2 \operatorname{H}_2(g) \rightleftharpoons \operatorname{Sn}(s) + 2 \operatorname{H}_2O(g)$$
  $\operatorname{K} = 8.12$   
 $2 \operatorname{CO}(g) + 2 \operatorname{H}_2O(g) \rightleftharpoons 2 \operatorname{H}_2(g) + 2 \operatorname{CO}_2(g)$   $\operatorname{K} = \frac{1}{(0.771)^2}$   
 $\operatorname{SnO}_2(s) + 2 \operatorname{CO}(g) \rightleftharpoons \operatorname{Sn}(s) + 2 \operatorname{CO}_2(g)$   $\operatorname{K} = \left(8.12\right) \left(\frac{1}{(0.771)^2}\right)$ 

For this reaction, K=13.7

## 7. Evaluation of the Value of K

## Question

The equilibrium constant for the formation of gaseous lithium iodide by combination of the elements in the gas phase at 3000 K is given as:

$$Li(g) + \frac{1}{2}I_2(g) \rightleftharpoons LiI(g)$$
  $K_p = 644$ 

- (a) What is the equilibrium constant value for this reaction if it is represented by the equation given above multiplied by a factor of 2?
- (b) What is the equilibrium constant value for the reverse of the reaction as written above?

#### **Solution**

(a) Multiplying the reaction by a factor of 2 requires that the given value of  $K_p$  be squared:

$$K_p = (644)^2 = 4.15 \times 10^5$$

$$2 \operatorname{Li}(g) + \frac{1}{2} \operatorname{I}_{2}(g) \rightleftharpoons 2 \operatorname{LiI}(g) \quad K_{p} = (644)^{2}$$

(b) When the equation is reversed,  $K_p$  becomes the reciprocal of the original value:  $K_p = \frac{1}{644}$   $K_p = \frac{1}{644} = 1.55 \times 10^{-3}$ 

This value of  $K_p$  is for the equation:  $LiI(g) \rightleftharpoons Li(g) + \frac{1}{2}I_2(g)$ 

## 8. Reaction Quotient

#### **Problem**

The concentration equilibrium constant  $(K_c)$  for the reaction

$$ClF_3(g) \rightleftharpoons ClF(g) + F_2(g)$$

is 8.77 x  $10^{-14}$  at 25 °C. Describe what happens quantitatively when a solution is prepared so that it is 17.50 M in ClF<sub>3</sub>, 1.3 x  $10^{-6}$  M in ClF, and 4.72 x  $10^{-7}$  M in F<sub>2</sub>.

## **Approach**

Calculate the reaction quotient, Q, and compare it to K.

#### **Solution**

The reaction quotient for the solution is:

$$Q = \frac{[C1F][F_2]}{[C1F_3]} = (1.3 \times 10^{-6} \text{ M}) \frac{(4.72 \times 10^{-7} \text{ M})}{(17.50 \text{ M})} = 3.5 \times 10^{-14}$$

 $Q < K_c$ , therefore the concentrations of the reactants will decrease and those of the products will increase, and the reaction will proceed toward equilibrium in the forward direction. In this case,  $ClF_3$  will decompose until equilibrium is reached.

## 9. Equilibrium Concentrations

## Question

Chlorine gas,  $Cl_2$ , dissociates into chlorine atoms in a reversible reaction for which K = 0.37 at 3000 K. What is the concentration of chlorine atoms in a vessel that originally contained 1.0 M of molecular chlorine?

## **Approach**

First, write the balanced equation. Then write the corresponding equilibrium expression and identify what is unknown. Make a table to include the chemical equation, initial concentrations, changes in concentration, and equilibrium concentrations. Substitute the equilibrium concentrations from the table into the equilibrium expression and solve for the unknown (x). If an approximation was made, remember to check for validity. Finally, answer the question in the problem using some form of the value of x.

#### **Solution**

The reaction is  $Cl_2(g) \rightleftharpoons 2 \ Cl(g)$ . The unknown is [Cl] at equilibrium, and we choose the concentration of  $Cl_2$  that dissociates into Cl as x. The algebraic expression that must be solved for is found by arranging the known and the unknown as shown in this lesson.

	$Cl_2$	$\rightleftharpoons$	2 Cl(g)
Initial	1.0 M		0 M
Change	- X		+ 2x
Equilibrium	1.0 - x		2x

The equilibrium constant is represented as:

$$K = \frac{[C1]^2}{[C1_2]} = \frac{(2x)^2}{(1.0 - x)} = 0.37$$

Inspection shows that the values of K and the known concentration are similar in magnitude, therefore this problem should be solved using the quadratic equation.

$$4x^2 = (0.37)(1.0 - x)$$
$$4x^2 + 0.37x - 0.37 = 0$$

With a = 4, b = 0.37, and c = -0.37, the quadratic equation is:

$$\frac{-0.37 \pm \sqrt{(0.37)^2 - (4)(4)(-0.37)}}{(2)(4)}$$

$$\frac{-0.37 \pm 2.5}{8}$$

x = 0.27 M or -0.36 M Negative answers do not work in chemistry!

Therefore,  $[C1]_2 = 2x = (2)(0.27 \text{ M}) = 0.54 \text{ M}.$ 

Finally, check this answer by substituting all concentrations into the equilibrium expressions and compare.

$$K = \frac{[C1]^2}{[C1_2]} = \frac{(0.54)^2}{(1.0 - 0.27)} = 0.40$$

## 10. Le Chatelier's Principle: Factors That Influence Equilibria - Concentration

## **Problem**

A reaction of potassium chromate and hydrochloric acid was allowed to come to equilibrium:

$$2 \text{ CrO}_4^{2^-} + \text{ H}^+ \rightleftharpoons \text{ Cr}_2 \text{O}_7^{2^-} + \text{ H}_2 \text{O}(\ell)$$

chromate ion dichromate ion yellow orange

Describe the changes that will occur in the equilibrium system when:

- (a) additional acid is added
- (b) additional potassium chromate is added
- (c) zinc is added (note that ZnCrO<sub>4</sub> is highly insoluble and ZnCr<sub>2</sub>O<sub>7</sub> is very soluble)
- (d) NaOH is added

## **Solution**

- (a) Some of the additional H<sup>+</sup> will react with the remaining chromate ion to produce more dichromate ion and water. [CrO<sub>4</sub><sup>2</sup>-] will decrease and [Cr<sub>2</sub>O<sub>7</sub><sup>2</sup>-] will increase.
- (b) Some of the additional chromate ion will react with some of the H<sup>+</sup> to produce more dichromate ion. Water and [H<sup>+</sup>] will decrease.
- (c) Addition of Zn<sup>2+</sup> will remove some of the chromate ion as ZnCrO<sub>4</sub>. This will lower the concentration of chromate ion. Thus, some of the dichromate ion will react to form additional chromate ion and H<sup>+</sup>.
- (d) Addition of NaOH will remove some of the H<sup>+</sup> as a result of an acid-base reaction. The decrease in [H<sup>+</sup>] will yield a reaction of additional  $Cr_2O_7^{2-}$  with  $H_2O$ . [ $Cr_2O_7^{2-}$ ] will decrease and [ $CrO_4^{2-}$ ] will increase.

# 11. Le Chatelier's Principle: Factors That Influence Equilibria -Temperature and Pressure Question

For the reaction

$$2 \text{ Hg(l)} + O_2(g) \rightleftharpoons 2 \text{ HgO(s)}$$

 $\Delta H^{\circ}$  = - 180.7 kJ over a temperature range of 298 K to 500 K.  $K_p$  = 3.2 x 10<sup>20</sup> at 298 K.

- (a) Is the value of  $K_p$  at 500 K expected to be greater or less than the value of  $K_p$  at 298 K?
- (b) Will a decrease in the partial pressure of O<sub>2</sub> cause the reaction to shift to the left or to the right?

#### **Solution**

(a) This is an exothermic reaction, thus heat can be considered a "product."

$$2 \operatorname{Hg}(1) + \operatorname{O}_2(g) \rightleftharpoons 2 \operatorname{HgO}(s) + 180.7 \text{ kJ}$$

Increasing the temperature favors the endothermic reaction, or the reverse reaction in this case. Therefore, the equilibrium will be shifted toward the reactant side (left) as the temperature is increased. The value of  $K_p$  is expected to be less than  $3.2 \times 10^{20}$ . (The value of  $K_p$  at  $500 \times 5.1 \times 10^{-7}$ .)

(b) Decreasing the pressure favors an increase in the amount of gas present. In this case, the reverse reaction (shift to the left) would be favored.

## 12. Le Chatelier's Principle: Factors That Influence Equilibria - Concentration, Temperature, and Volume

**Problem** The value of  $K_p$  for the following reaction is 0.16 at 25 °C. The enthalpy change for the reaction at standard conditions is +16.1 kJ.

$$2 \text{ NOBr}(g) \rightleftharpoons 2 \text{ NO}(g) + \text{Br}_2(g)$$

To which direction will the equilibrium shift (left, right, or no change) and how will K change when each of the following changes to the system is made?

- (a) Adding more Br<sub>2</sub>(g)
- (b) Removing some NOBr(g)
- (c) Decreasing the temperature
- (d) Increasing the container volume

## **Approach**

This is an endothermic reaction, thus heat is considered a "reactant."

+ 
$$16.1 \text{ kJ} + 2 \text{ NOBr}(g) \rightleftharpoons 2 \text{ NO}(g) + \text{Br}_2(g)$$

#### **Solution**

- (a) Left. Some of the added "product" will be consumed, thus the equilibrium will shift to the left. There will be no change in K.
  - (b) Left. Here, a "reactant" is being depleted. The equilibrium will shift to the left. K will not change.
- (c) Left. When the temperature decreases, the system responds by shifting in the direction that leads to generation of thermal energy. The equilibrium shifts left and the value of K decreases.
- (d) Right. Increasing the volume of the flask will result in a shift to the side of the equilibrium with more gas molecules. There are three moles of gas on the right and only two on the left. K will not change.

## 13. Free Energy and Equilibrium

#### **Problem**

Calculate the equilibrium constant for the reaction shown in problem 1.

$$CCl_4(1) + H_2(g) \rightarrow HCl(g) + CHCl_3(1)$$

 $\Delta G^{\circ}$  is -103.7 kJ at 25 °C for this reaction.

## **Solution**

The following equation shows the relationship between  $\Delta G^{\circ}$  and the equilibrium constant, K.

$$\Delta G^{\circ} = -RT \ln K, \text{ where } R = 8.3145 \text{ J/(K mol)}$$

$$\ln K = -\frac{\Delta G^{\circ}}{RT} = -\frac{(-103.7 \text{ kJ}) \left(\frac{1000 \text{ J}}{1 \text{ kJ}}\right)}{(8.314 \text{ J/K·mol})(298 \text{ K})} = 41.86$$

$$K = 1.5 \times 10^{18}$$

Under standard state conditions at 25 °C, this reaction is spontaneous and the products are highly favored over the reactants at equilibrium.