# Chemical Kinetics: The Rates of Chemical Reactions

Chapter 12



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Chemistry 222

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# **Shroud of Turin**

Shroud of Jesus?!? Fake or Real? Explored with Kinetics







# **Chemical Kinetics**

- We can use thermodynamics to tell if a reaction is product or reactant favored.
- But this gives us no info on HOW FAST reaction goes from reactants to products.
- KINETICS the study of REACTION RATES and their relation to the way the reaction proceeds, i.e., its MECHANISM.

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# Reaction rate is the change in concentration of a

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reactant or product with time Ex: for  $\mathbf{A} \rightarrow \mathbf{B}$ 



**Reaction Rates** 

# **Reaction Rates**

Reaction rate is the change in concentration of a reactant or product with time

Reactants *disappear* with time (hence, negative sign), and products *appear* with time (hence, positive sign)

Ex: for 
$$N_2O_{4(g)} \rightarrow 2 NO_{2(g)}$$

$$rate = -\frac{\Delta[N_2O_4]}{\Delta t} = +\frac{1}{2}\frac{\Delta[NO_2]}{\Delta t}$$

Rates in chemistry are usually "amount per unit time", i.e. M/s, etc. MAR





## **Determining a Reaction Rate**



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# Average, Instantaneous, Reaction Rates



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### We will use "average rate" in CH 222

**Factors Affecting Rates** 

#### Concentration

Greater concentration of reactants means more collisions and faster rates

#### Temperature

Higher temperatures means particles collide with greater kinetic energy, increasing the rates

#### Surface Area

Increased surface area means greater chances for collisions and faster rates

#### Catalysts

Catalysts speed up reactions without being used up. They lower the activation energy and increase the rates

### Factors Affecting Rates



### **Factors Affecting Rates**

### Surface area of reactants





Lycopodium powder is a yellow-tan dust-like powder consisting of the dry spores of clubmoss plants or ferns MAR

### **Factors Affecting Rates**

Catalysts: catalyzed decomposition of  $H_2O_2$  with  $MnO_2$ 



 $2 H_2O_2(l) \longrightarrow 2 H_2O(l) + O_2(g)$ 

# **Factors Affecting Rates**

Temperature



# **Concentrations and Rates**

To postulate a reaction mechanism, we study its reaction rate and concentration dependence



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# **Concentrations and Rates**

Take reaction where CI<sup>.</sup> in cisplatin [Pt(NH<sub>3</sub>)<sub>2</sub>Cl<sub>2</sub>] is replaced by H<sub>2</sub>O



Rate of change of conc of Pt compd $= \frac{Am't of cisplatin reacting (mol/L)}{elapsed time (t)}$ 

# **Concentrations and Rates**

 $\frac{Rate \text{ of change of conc of Pt compd}}{\frac{Am't \text{ of cisplatin reacting (mol/L)}}{\text{ elapsed time (t)}}}$ 

If calculated rate = 4.3 x 10<sup>-6</sup> M s<sup>-1</sup> and [cisplatin] = 0.00250 M, then approximate time for cisplatin to react:

rate = [cisplatin] / time, and time = [cisplatin] / rate time = 0.00250 M / 4.3 x 10<sup>-6</sup> M s<sup>-1</sup> time = 580 s



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k is independent of conc. but increases with T



a A + b B ---> x X with a catalyst C

Rate = k [A]<sup>m</sup>[B]<sup>n</sup>[C]<sup>p</sup>

The exponents m, n, and p

- are the reaction order
- can be 0, 1, or 2 (in CH 222 CH 223!)
- · must be determined by experiment!
- overall order = m + n + p

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# 34 ... Interpreting Rate Laws

Example: Rate = k [A] <sup>m</sup> If m = 1, rxn. is 1st order in A		<i>Example:</i> Derive rate law and k for CH <sub>3</sub> CHO(g)> CH₄(g) + CO(g)			
Rate = k [A] <sup>1</sup> If [A] doubles, then rate goes up by factor of ?	from experimental data for rate of disappearance of CH <sub>3</sub> CHO				
If $m = 2$ , rxn. is 2nd order in A.		Expt.	[CH₃CHO] (mol/L)	Disappear of CH₃CHO (mol/L•sec)	
Rate = $k [A]^2$		1	0.10	0.020	
Doubling [A] increases rate by ?		2	0.20	0.081	
lf m = 0, rxn. is zero order.		3	0.30	0.182	
Rate = k [A] <sup>0</sup>		4	0.40	0.318	
If [A] doubles, rate ?	MAR	TI	ne rate law:	rate = k[CH₃CHO]×	

# **Deriving Rate Laws**

#### Expt. [CH<sub>3</sub>CHO] (mol/L) Rate of CH<sub>3</sub>CHO (mol/L•sec)

1	0.10	0.020
2	0.20	0.081
3	0.30	0.182
4	0.40	0.318

Let's find the order (x) with respect to CH<sub>3</sub>CHO Use two trials where [CH<sub>3</sub>CHO] changes - any change in rate is caused by CH<sub>3</sub>CHO

Apply the rate law to these two trials:

So the order of reaction for CH<sub>3</sub>CHO is "2". We say the reaction is second order with respect to CH<sub>3</sub>CHO

# 34 ... Deriving Rate Laws

😹 📥 Deriving Rate Laws

### Rate of rxn = k [CH₃CHO]<sup>2</sup>

- Here the rate goes up by \_\_\_\_\_ when initial conc. doubles. Therefore, we say this reaction is order.
- Now determine the value of k. Use expt. #3 data on earlier slide.

0.182 mol/L•s = k (0.30 mol/L)<sup>2</sup>

#### $k = 2.0 (L / mol \cdot s)$

Using k you can calc. rate at other values of [CH<sub>3</sub>CHO] at same T.

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# Concentration/Time Relations

Chemists need to know what the concentration of reactant is as function of time.

*Most* reactions are first order (radioactive, biological, etc.)

Let's consider FIRST ORDER REACTIONS

For 1st order reactions (1), the rate law is:

- ( $\Delta$  [R] /  $\Delta$  time) = k [R]<sup>1</sup>

Integration (calcul

on (calculus): 
$$\int_0^t \frac{1}{[R]} dR = -k \int_0^t dt$$

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### Concentration/Time Relations

Integrating  $-(\Delta [R] / \Delta time) = k [R]$  we get:

0

This is the integrated first-order rate law.

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#### Sucrose decomposes to simpler sugars Rate of disappearance of sucrose = k [sucrose]

k = 0.21 hr-1

Initial [sucrose] =

0.010 M

How long to drop 90% (to 0.0010 M)?

**Concentration/Time Relations** 

Rate of disappear of sucrose = k [sucrose], k = 0.21 hr<sup>-1</sup>. If initial [sucrose] = 0.010 M, how long to drop 90% or to 0.0010 M?

### Use the first order integrated rate law

$$\ln\left(\frac{0.0010 \text{ M}}{0.010 \text{ M}}\right) = -(0.21 \text{ hr}^{-1}) \text{ t}$$

 $\ln (0.10) = -2.30 = -(0.21 \text{ hr}^{-1}) \cdot \text{time}$ time = 11 hours

sig figs and logarithms covered in CH 223

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### Using the Integrated Rate Law

The integrated rate law suggests a way to tell if a reaction is first order based on experiment.

 $2 N_2O_5(g) ---> 4 NO_2(g) + O_2(g)$ Rate = k[N<sub>2</sub>O<sub>5</sub>]

Time (min)	[N <sub>2</sub> O <sub>5</sub> ] (M)	In [N <sub>2</sub> O <sub>5</sub> ]
0	1.00	0
1.0	0.705	-0.35
2.0	0.497	-0.70
5.0	0.173	-1.75

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## Using the Integrated Rate Law

### $2 N_2 O_5(g) \longrightarrow 4 NO_2(g) + O_2(g) Rate = k[N_2 O_5]$



Data of conc. vs. time plot do not fit straight line.



Plot of In [N<sub>2</sub>O<sub>5</sub>] vs. time is a straight line!

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### Using the Rate Laws

Characteristic Properties of Reactions of the Type "R $\longrightarrow$ Products"					
Order	Rate Equation	Integrated Rate Equation	Straight-Line Plot	Slope	k Units
0	$-\Delta[\mathbf{R}]/\Delta \mathbf{T} = k[\mathbf{R}]^0$	$[R]_0 - [R]_t = kt$	[R] <sub>t</sub> vs. t	-k	mol/L ∙ time
1	$-\Delta[\mathbf{R}]/\Delta \mathbf{T} = k[\mathbf{R}]^1$	$\ln ([R]_t/[R]_0) = -kt$	ln [R] <sub>t</sub> vs. t	-k	time <sup>-1</sup>
2	$-\Delta[\mathbf{R}]/\Delta \mathbf{T} = k[\mathbf{R}]^2$	$(1/[R]_t) - (1/[R]_0) = kt$	1/[R] <sub>t</sub> vs. t	k	L/mol∙time

Also see the "Kinetics Cheat Sheet" Handout

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y = ax + b

rate const conc at = slope time = 0



All 1st order reactions have straight line plot for In [R] vs. time.

(2nd order gives straight line for plot of 1/[R] vs. time; zero order [R] vs. time) - see Handout





## Half-Life

Reaction after 4 halflives, or 2616 min. 1/16 of the reactant remains.

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### Half-Life

Sugar is fermented in a 1st order process (using an enzyme as a catalyst).

sugar + enzyme --> products Rate of disappear of sugar = k[sugar] k = 3.3 x 10<sup>-4</sup> sec<sup>-1</sup>

What is the half-life of this reaction?



Half-Life

see <u>Handout</u>

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#### Half-Life

Rate = k[sugar] and k =  $3.3 \times 10^{-4}$  sec<sup>-1</sup>. Half-life is 35 min. Start with 10.00 g sugar. How much is left after 2 hr and 20 min? ( $t_{1/2}$  = 0.693 / k)

Two Solution pathways - The "CH 104" method:

2 hr and 20 min = 4 half-lives

Half-life	Time Elapsed	Mass Left
1st	35 min	5.00 g
2nd	70	2.50 g
3rd	105	1.25 g
4th	140	0.625 g answer

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### Half-Life

Rate = k[sugar] and k =  $3.3 \times 10^{-4}$  sec<sup>-1</sup>. Half-life is 35 min. Start with 10.00 g sugar. How much is left after 2 hr and 20 min? ( $t_{1/2}$  = 0.693 / k)

Two Solution Pathways - The "CH 222" Method:

Convert 2 hrs 20 min to 8400 seconds In (R / 10.00 g) = - ( $3.3 \times 10^{-4} \text{ sec}^{-1}$ )(8400 s) In (R / 10.00 g) = - 2.772 Take *antilog*: (R / 10.00 g) = e<sup>-2.772</sup> = 0.0625 R = 10.00 g \* 0.0625 = 0.625 g

CH 222 Method recommended,

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CH 222 Method recommended, not limited to whole number of half-lives, etc. e = "Euler's number" in math = 2.71828...

### Half-Life



### Half-Life

Start with 1.50 mg of tritium, how much is left after 49.2 years?  $t_{1/2} = 12.3$  years In [R] / [R]<sub>0</sub> = -kt [R] = ? [R]<sub>0</sub> = 1.50 mg t = 49.2 yrs Need k, so we calc k from: k = 0.693 /  $t_{1/2}$ Obtain k = 0.0564 y<sup>-1</sup> Now In [R] / [R]<sub>0</sub> = -kt = - (0.0564 y<sup>-1</sup>) • (49.2 y) = -2.77 Take antilog: [R] / [R]<sub>0</sub> = e<sup>-2.77</sup> = 0.0627 0.0627 is the fraction remaining [R]<sub>0</sub> = 1.50 mg, so [R] = 1.50\*0.0627 = 0.0941 mg

### Half-Life

Half-Life for first order reactions:

$$t_{1/2} = 0.693 / k$$

All biological, radioactive processes first order, most useful

Half-Life for second order reactions:

$$t_{1/2} = 1 / (k[A]_0)$$

Half-Life for zero order reactions:  $t_{1/2} = [A]_0 / 2k$ 

concentration of the reactant

[A]<sub>0</sub> is the initial

Half-Lives of Radioactive Elements

Rate of decay of radioactive is terms of half-life (t <sub>1/2</sub> ).	otopes given in
<sup>238</sup> U> <sup>234</sup> Th + He	4.5 x 10 <sup>9</sup> y
<sup>14</sup> C> <sup>14</sup> N + beta	5730 y
<sup>131</sup> I> <sup>131</sup> Xe + beta	8.05 d
Element 106 - seaborgium <sup>263</sup> Sg> <sup>259</sup> Rf + He	0.8 s
Element 111 - roentgenium <sup>272</sup> Rg> <sup>268</sup> Mt + He	0.0015 s

Half-life also used in medicine;  $t_{1/2}$  caffeine = 3.5 hours in the body

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#### MECHANISMS A Microscopic View of Reactions

How are reactants converted to products at the molecular level?

We want to connect the RATE LAW to the MECHANISM the experiment to the

theory

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# **Reaction Coordinate Diagrams**



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# **Reaction Coordinate Diagrams**



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# **Activation Energy**

There is a minimum amount of energy required for a reaction: the activation energy, Ea. In general, differences in activation energy are the reason reactions vary from fast to slow.



# **Temperature and Rate**



Generally, as temperature increases, so does the reaction rate.

This is because k is temperature dependent.

**Find activation energy** through changes in temperature.

**Effect of Temperature** 

Reactions generally occur slower at lower T.



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Iodine clock reaction H<sub>2</sub>O<sub>2</sub> + 2 I<sup>-</sup> + 2 H<sup>+</sup> --> 2 H<sub>2</sub>O + I<sub>2</sub>

**Collision Theory** 

To break and make bonds, reactions require (a) activation energy and (b) correct geometry.

 $O_3(g) + NO(g) ---> O_2(g) + NO_2(g)$ 



0 — 0 0 N = 0

Insufficient activation energy





# **Collision Theory**

To break and make bonds, reactions require (a) activation energy and (b) correct geometry.  $O_3(g) + NO(g) ---> O_2(g) + NO_2(g)$ 0 **=** N 0-0 Correct activation energy and geometry

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#### The Arrhenius Equation Arrhenius equation -Temp (K) $k = Ae^{-E_a/RT}$ Rate constant Svante Arrhenius Activation 8.3145 J/K•mol Frequency factor energy Frequency factor = frequency of collisions with correct geometry. Plot In k vs. 1/T ---> straight line. $\ln k = -(\frac{E_a}{R})(\frac{1}{T}) + \ln A$ straight line. slope = -E<sub>a</sub>/R, best way to fi best way to find E<sub>a</sub> MAR Always use 8.3145 for "energy" R!

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# Activation Energy and Temperature

Reactions are slower at lower T because a smaller fraction of reactant molecules have enough energy to convert to product molecules.



In general, differences in activation energy cause reactions to vary from fast to slow.

#### More About the Frequency Factor, A

Frequency Factor often expressed as:



We will be seeing entropy ( $\Delta$ S) again in CH 223.

# **REACTION MECHANISMS**





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# **MOLECULARITY**

The molecularity of a process tells how many molecules are involved in the elementary step.

UNIMOLECULAR - only one reactant is involved.

**BIMOLECULAR** - two different molecules must collide

TERMOLECULAR - three different molecules collide

Elementary Reactions and Their Rate Laws			
Molecularity	Elementary Reaction	Rate Law	
<i>Uni</i> molecular	$A \longrightarrow products$	Rate = $k[A]$	
<b>Bimolecular</b>	$A + A \longrightarrow products$	Rate = $k[A]^2$	
Bimolecular	$A + B \longrightarrow products$	Rate $= k[A][B]$	
Termolecular	$A + A + A \longrightarrow$ products	Rate = $k[A]^3$	
Termolecular	$A + A + B \longrightarrow products$	Rate = $k[A]^2[B]$	
Termolecular	$A + B + C \longrightarrow products$	Rate $= k[A][B][C]$	

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# **MECHANISMS**

Some reactions occur in a single elementary step. Most reactions involve a sequence of elementary steps.

Adding elementary steps gives NET reaction.





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# **MECHANISMS**

Most reactions involve a sequence of elementary steps.

Adding elementary steps gives NET reaction.

 $\mathsf{Bimolecular} \quad \mathsf{NH}_3 * \mathsf{OC1}^- \longrightarrow \mathsf{NH}_2\mathsf{C1} * \mathsf{OH}^-$ 

Step 2 Bimolecular NH₂Cl + NH₂ → N₂Hs\* + Cl<sup>-</sup> Step 3 Bimolecular  $N_2H_5^+ + OH^- \longrightarrow N_2H_4 + H_2O$ 

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H-N:

Every elementary step gets a "hump" in the diagram • Overall reaction  $2 \text{ NH}_3 + \text{OC1}^- \longrightarrow \text{N}_2\text{H}_4 + \text{H}_2\text{O} + \text{C1}^-$ 

Reaction Co-ordinate

# **Mechanisms**

In multistep mechanisms, one step will be slower than all others - this is the rate determining step (rds).

Most reactions involve a sequence of elementary steps. Example:

2 I + HOOH + 2 H + ---> I<sub>2</sub> + 2 H<sub>2</sub>O Rate = k  $[I^{-}]$   $[H_2O_2]$ 

Note that the rate law comes from experiment. Also note that order of reactants in rate law not necessarily the same as stoichiometric coefficients!

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### **MECHANISMS**

2 I <sup>.</sup> +	ноон	+ 2	H+	>	$I_2$	+	2 H₂O
	Rat	e = k	[ŀ]	[HO	он	]	

A scientist proposes the following mechanism for this reaction:

Step 1 - slow	HOOH + I> HOI + OH
Step 2 - fast	HOI + I <sup>-</sup> > $I_2$ + OH <sup>-</sup>
Step 3 - fast	2 OH <sup>-</sup> + 2 H <sup>+</sup> > 2 H <sub>2</sub> O

Note that H<sup>+</sup> not involved in slow step, so [H<sup>+</sup>] is not in the rate law (a zero order reactant.)

Bimolecular slow step reflected in the rate law; this is a legitimate mechanism.

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2 I' + HOOH + 2 H' ---> I<sub>2</sub> + 2 H<sub>2</sub>O Rate = k [I-] [HOOH] Step 1 - slow HOOH + I --> HOI + OH Step 2 - fast HOI + I --> I<sub>2</sub> + OH Step 3 - fast 2 OH + 2 H+ --> 2 H<sub>2</sub>O



Step 1 is bimolecular and involves I- and HOOH. Therefore, this predicts the rate law should be Rate  $\alpha$  [I·] [HOOH] - as observed!!

### The species HOI and OH- are reaction

intermediates; critical for providing evidence for or against a proposed mechanism. See: Reaction Mechanisms Guide

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# **Mechanisms - Uses** Mechanisms help predict the products of a reaction Very useful in organic chemistry: the S<sub>N</sub>1 and S<sub>N</sub>2 mechanisms



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# **CATALYSIS**

### Catalysts speed up reactions by altering the mechanism to lower the activation energy barrier.





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Page III-12-11 / Chapter Twelve Lecture Notes

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SPENT/20 MINUTESTRYING TO UNDERSTAND A KINETICS PROBLEM

HOURS







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# End of Chapter 12 FORGOT TO CHANGE MINUTES TO

#### See<sup>.</sup>

- Chapter Twelve Study Guide
- <u>Chapter Twelve Concept Guide</u>
- · Important Equations (following
- this slide) End of Chapter Problems
- (following this slide)

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#### End of Chapter Problems: Test Yourself

- The reaction between ozone and nitrogen dioxide at 231 K is first order in both NO<sub>2</sub> and O<sub>3</sub>: 2 NO<sub>2</sub>(g) + O<sub>3</sub>(g) → N<sub>2</sub>O<sub>5</sub>(s) + O<sub>2</sub>(g) Write the rate equation for the reaction. If the concentration of NO<sub>2</sub> is tripled, what is the change in the reaction rate?
   After 2.57 h at 27 °C, a first order sucrose concentration decreased from 0.0146 M to 0.0132 M. Find the rate constant, k.
- 3.
- 0.0146 M to 0.0132 M. Find the rate constant, K. The compound Xe(CF<sub>3</sub>) decomposes in a first-order reaction to elemental Xe with a half-life of 30. min. If you place 7.50 mg of Xe(CF<sub>3</sub>)<sub>2</sub> in a flask, how long must you wait until only 0.25 mg of Xe(CF<sub>3</sub>)<sub>2</sub> remains? Gaseous NO<sub>2</sub> decomposes at 573 K: 2 NO<sub>2</sub>(g)  $\rightarrow$  2 NO(g) + O<sub>2</sub>(g) The concentration of NO<sub>2</sub> was measured as a function of time. A graph of 1/ 4.
- $[NO_2]$  versus time gives a straight line with a slope of 1.1 L/mol.s. What is the rate law for this reaction? What is the rate constant k?
- the rate raw not this reaction? What is the rate constant K? S What is the rate law for the following *elementary* reaction: NO(g) + NO<sub>3</sub>(g) → 2 NO<sub>2</sub>(g) 6. For a reaction, In k versus 1/T(K) is plotted, and the linear regression line is: y = -6373.3x + 18.19, r = -0.997 What is the activation energy for this reaction?

#### Important Equations, Constants, and Handouts from this Chapter:

The Rate Law:  $Rate = k[A]^p[B]^m[C]^n \dots$ m, n, p = 0, 1 or 2 only (in our classes)

Order Integrated Rate Law;  

$$ln \frac{[R]}{R} = -kt$$

1st (

$$\begin{bmatrix} R_0 \end{bmatrix} \\ t_{\frac{1}{2}} = \frac{0.693}{k}$$

The Arrhenius Equation:  

$$ln(k) = -\left(\frac{E_a}{R}\right)\left(\frac{1}{T}\right) + ln(A)$$

• R = 8.3145 J/mol·K

- "Kinetics Cheat Sheet"
- handout
- "Reactions Mechanisms" handout

Kinetics: rate, rate law, orders of reaction, the rate constant (k), 1st vs. 2nd. vs. zero order, half life, mechanism, elementary reaction, bimolecular (and uniand ter-molecular), Arrhenius equation, activation energy, frequency factor, mechanism, intermediate, catalyst, rds (rate determining step)

#### End of Chapter Problems: Answers

- Rate = k[NO2][O3]; tripling NO triples the rate. 0.0392 h<sup>-1</sup>
- 2. 3.
- 150 min Rate =  $k[NO_2]^2$ , k = 1.1 L/mol·s Rate =  $k[NO][NO_3]$
- 4. 5.
- 6. 53.0 kJ/mol