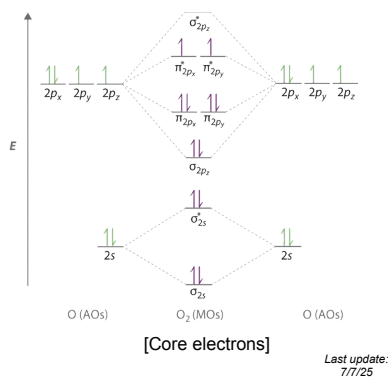


## Chapter 5: Advanced Theories of Bonding

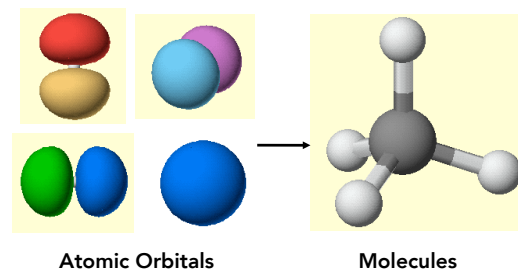
Chemistry 221  
Professor Michael Russell  
<http://mhchem.org/221>

MAR



### 5.1 - Valence Bond Theory

How to go from atomic orbitals to the geometries described via VSEPR in molecules?



MAR

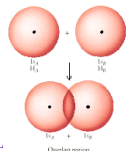
### Two Theories of Bonding

#### VALENCE BOND (VB) THEORY -

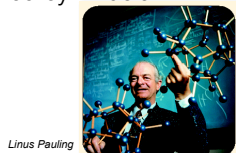
Linus Pauling

valence electrons are **localized** between atoms (or are **lone pairs**)  
half-filled atomic orbitals overlap to form bonds.

electrons stabilized by 2 nuclei

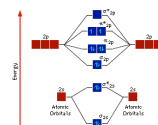


MA



#### MOLECULAR ORBITAL (MO) THEORY - Robert Mulliken

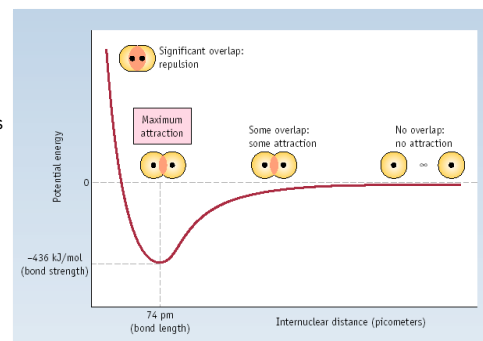
valence electrons are **delocalized** over entire molecule in **molecular orbitals**



### Sigma Bonds

For both theories, consider the 'overlap' between orbitals to make a sigma ( $\sigma$ ) bond

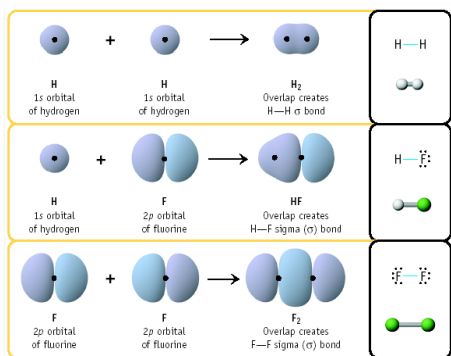
This diagram is for two 1s orbitals ( $H_2$ )



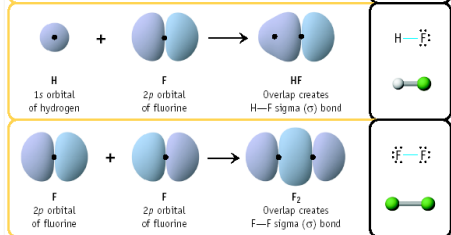
MAR

### Other Types of Sigma Bonds

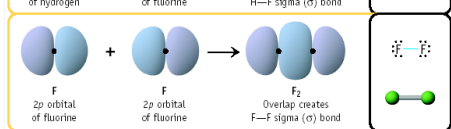
Two s orbitals overlap



One s & one p overlap



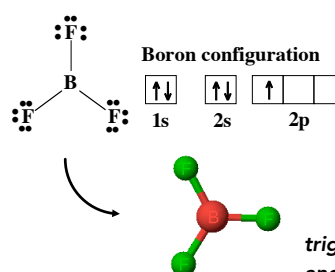
Two p orbitals overlap



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### 5.2 - Hybrid Atomic Orbitals

Bonding in  $BF_3$

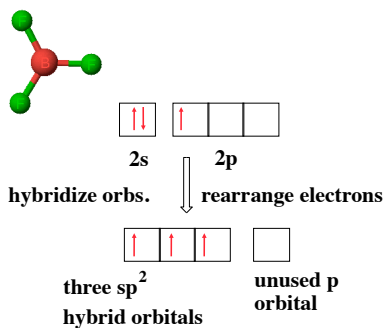


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We can use  $BF_3$  to discuss Valence Bond Theory.

The question:

How to account for 3 bonds  $120^\circ$  apart using a spherical s orbital and p orbitals that are  $90^\circ$  apart?

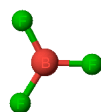
Valence Bond Theory: Bonding in  $\text{BF}_3$ 

MAR

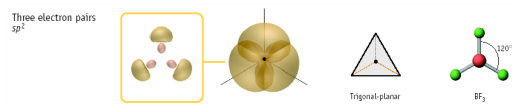
Pauling said to modify  
Valence Bonds with **Orbital Hybridization**

Mix available atomic orbitals  
to form a new set of orbitals  
- **Hybrid Orbitals** - that will  
give the maximum overlap  
in the correct geometry.

one s and 2 p atomic orbitals  
gives 3  $sp^2$  orbitals

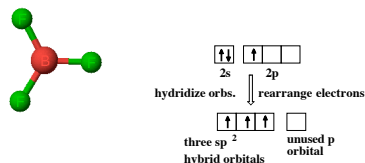
Valence Bond Theory: Bonding in  $\text{BF}_3$ 

The three hybrid orbitals are made from 1 s  
orbital and 2 p orbitals create 3  $sp^2$  hybrid orbitals

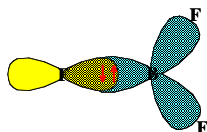


Now we have 3, half-filled HYBRID orbitals that  
can be used to form *planar* B-F sigma bonds.

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Valence Bond Theory: Bonding in  $\text{BF}_3$ 

An atomic orbital from each F overlaps one  
of the  $sp^2$  hybrids to form a B-F  $\sigma$  bond.

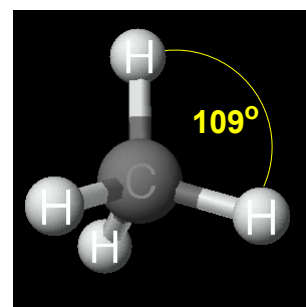


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Valence Bond Theory: Bonding in  $\text{CH}_4$ 

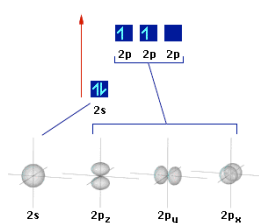
How do we account  
for 4 C-H sigma  
bonds  $109^\circ$  apart?

Need to use 4 atomic  
orbitals - s,  $p_x$ ,  $p_y$ ,  
and  $p_z$  - to form 4  
new hybrid orbitals  
pointing in the  
correct direction.



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## Bonding in a Tetrahedron - Formation of Hybrid Atomic Orbitals

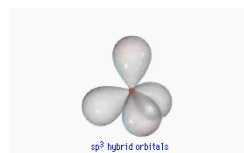


4 C atom orbitals  
hybridize to  
form four  
equivalent  $sp^3$   
hybrid atomic  
orbitals.

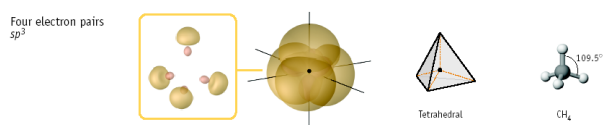
one s and 3 p atomic  
orbitals gives 4  $sp^3$   
orbitals

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## Bonding in a Tetrahedron - Formation of Hybrid Atomic Orbitals

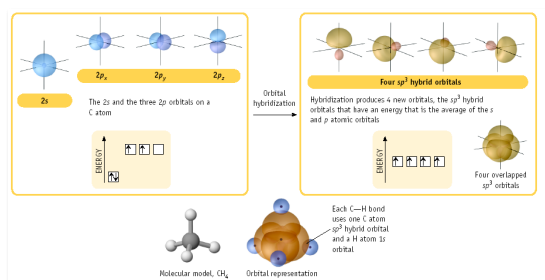


4 C atom orbitals  
hybridize to form four  
equivalent  $sp^3$  hybrid  
atomic orbitals.



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## Bonding in CH<sub>4</sub>



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## Valence Bond Theory: Summary

To form a covalent bond, an atom must have an **unpaired electron**.

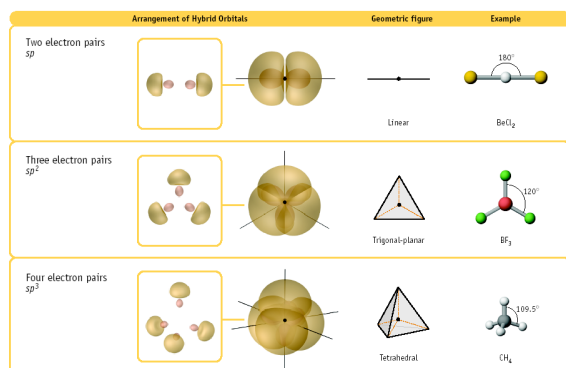
**Number of bonds** formed by an atom is **determined by the number of unpaired electrons**.

VB works well for explaining the bonding in diatomic molecules and for explaining the lack of bonding by the noble gases.

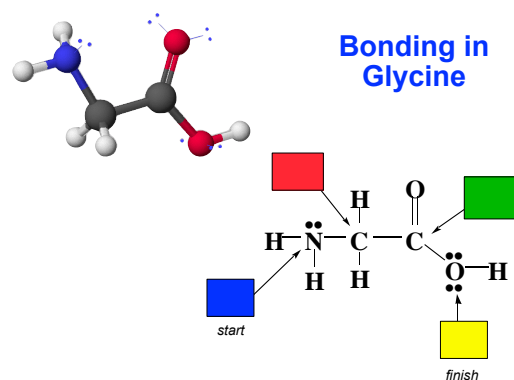
Bonds	EPG	Hybrid	Remaining p orbs?
2	linear	$sp$	2 p
3	trigonal planar	$sp^2$	1 p
4	tetrahedral	$sp^3$	none
5	trigonal bipyramid	$sp^3d$	---
6	octahedral	$sp^3d^2$	---

All tetrahedral EPG =  $sp^3$  hybridized, etc.

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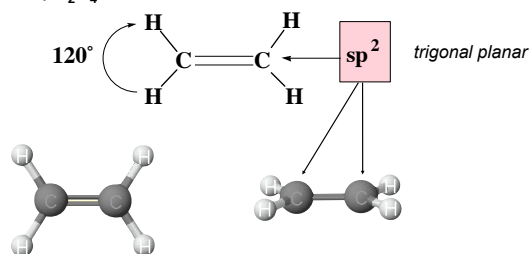


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## 5.3 - Multiple Bonds

How to multiple bonds work with valence bond theory?

Consider **ethylene**, C<sub>2</sub>H<sub>4</sub>

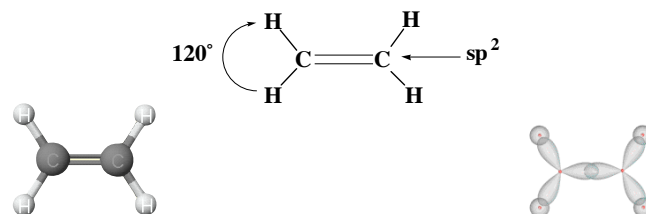


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## Sigma Bonds in C<sub>2</sub>H<sub>4</sub>

Sigma bonds ('single bonds') operate through 'head to head' overlap of singly occupied orbitals in each atom

Ethylene has sigma bonds between the C and H atoms as well as a sigma bond between the two C atoms

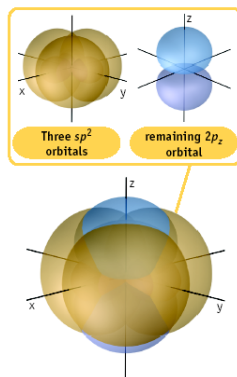
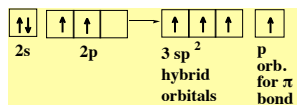


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Pi ( $\pi$ ) Bonds in  $C_2H_4$ 

The unused p electrons on each C overlap in a 'side-by-side' sharing of 'regular' atomic p orbitals to make a  $\pi$  bond

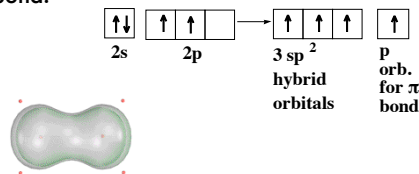
$\pi$  bonds are 'above and below' the sigma bond



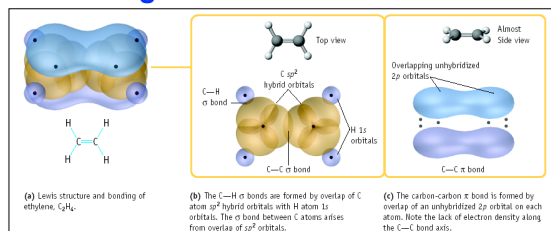
MAR

Pi ( $\pi$ ) Bonds in  $C_2H_4$ 

The unused p orbital on each C atom contains an electron, and this p orbital overlaps the p orbital on the neighboring atom to form the  $\pi$  bond.

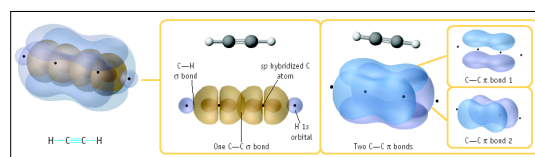


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Multiple Bonding in  $C_2H_4$ 

Notice how a double bond contains one sigma and one pi bond!

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 $\sigma$  and  $\pi$  Bonding in  $C_2H_2$ 

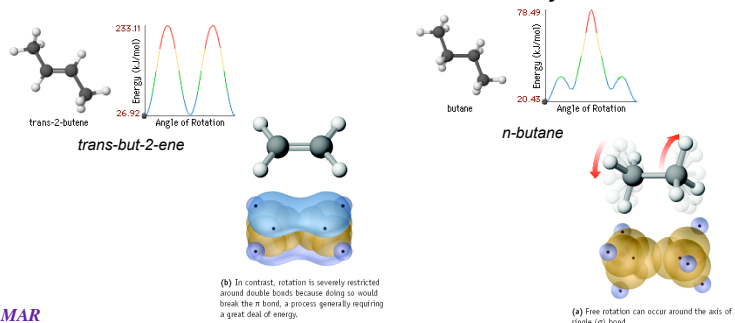
$C_2H_2$  has a triple bond

Notice how a triple bond contains one sigma and two pi bonds!

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## Consequences of Multiple Bonding

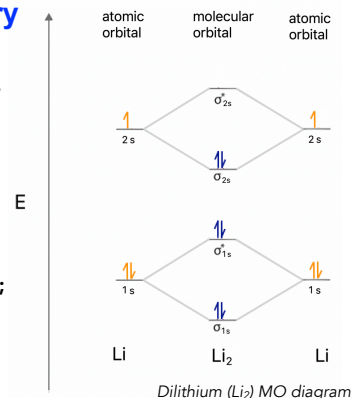
$C=C$  bonds do not rotate well, but  $C-C$  bonds rotate easily



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## 5.4 - Molecular Orbital Theory

**Molecular Orbital Theory (MO)** extends quantum mechanical wave functions to molecules  
MO accounts for paramagnetism, color, bonding  
Atomic orbitals delocalize into **molecular orbitals**  
**Bonding and Antibonding** orbitals  
Quite complicated, need computers;  
we will only look at **diatomics** (2 atom systems) from the **first and second periods only**



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## Advantages of MO Theory



Dioxygen should be electron paired (*diamagnetic*) by VB Theory, but dioxygen is actually *paramagnetic*. MO Theory accounts for paramagnetism of  $O_2$

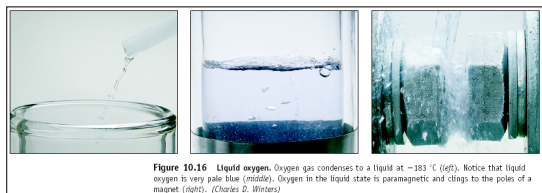


Figure 10.16 Liquid oxygen. Oxygen gas condenses to a liquid at  $-183^\circ\text{C}$  (left). Notice that liquid oxygen is very pale blue (middle). Oxygen in the liquid state is paramagnetic and clings to the poles of a magnet (right). (Charles D. Winters)

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## Four Principles of MO Theory

Principle #1:

Number of Molecular Orbitals =  
Number of Atomic Orbitals

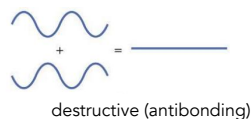
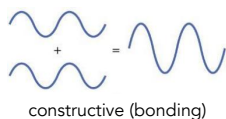
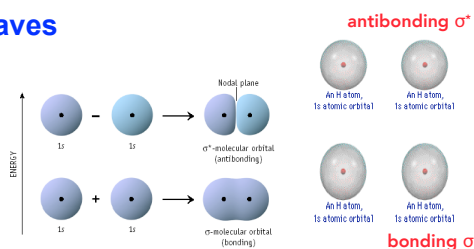
Two 1s orbitals from two hydrogen atoms  
create two molecular orbitals in  $H_2$

Two 1s orbitals and two 2s orbitals from two  
lithium atoms create four molecular orbitals in  $Li_2$

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## MO Theory and Waves

When two atomic 1s  
H orbitals combine,  
a **bonding ( $\sigma$ )** and  
**antibonding ( $\sigma^*$ )**  
molecular orbital  
forms



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## Principles #2 and #3 of MO Theory

Principle #2:

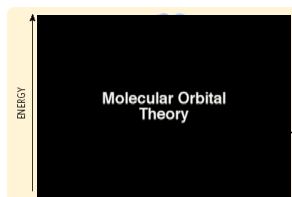
Bonding MO lower in energy than the parent orbital  
Antibonding MO higher in energy  
than the parent orbital

Principle #3:

Electrons of molecule assigned to  
successively higher MOs

Use *Pauli Exclusion Principle* and *Hund's Rule*  
when assigning electrons

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MO Diagram for  $H_2$ 

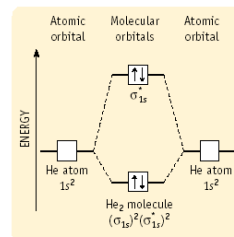
Antibonding MO

Atomic Orbitals

Bonding MO

Two 1s electrons from two H atoms  
occupy the  $\sigma$  orbital in  $H_2$

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MO Diagram for  $He_2$ 

Antibonding MO

Atomic Orbitals  
Bonding MO

Two 1s electrons in  $\sigma$ ,  
Two 1s electrons in  $\sigma^*$

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## Bond Order for H<sub>2</sub>

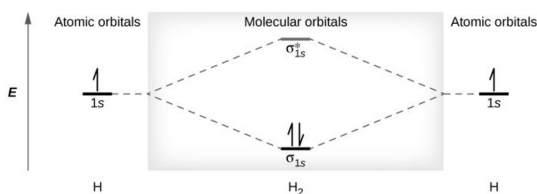
$$\text{Bond Order} = \frac{1}{2} (\# \text{ bonding } e^- - \# \text{ antibonding } e^-)$$

Bond Order > 0,

**stable molecule (exists)**

Bond Order = 0 (or < 0),

**unstable molecule (does not exist)**



Scientists use **bond order** to tell if a molecule can exist (or not)

*In H<sub>2</sub>,*  
 $\text{Bond Order} = \frac{1}{2} (2 - 0) = 1;$   
**stable**

## Bond Order for He<sub>2</sub>

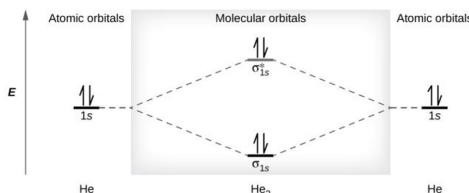
$$\text{Bond Order} = \frac{1}{2} (\# \text{ bonding } e^- - \# \text{ antibonding } e^-)$$

Bond Order > 0,

**stable molecule (exists)**

Bond Order = 0 (or < 0),

**unstable molecule (does not exist)**



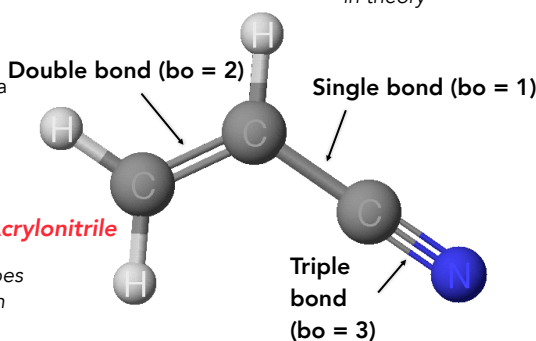
Scientists use **bond order** to tell if a molecule can exist (or not)

*In He<sub>2</sub>,*  
 $\text{Bond Order} = \frac{1}{2} (2 - 2) = 0;$   
**unstable**  
 $\therefore \text{He}_2 \text{ does not exist}$

## More on Bond Order

In a **Lewis structure**:

- \* a single bond has a bond order of 1
- \* a double bond has a bond order of 2
- \* a triple bond has a bond order of 3



**Acrylonitrile**

As bond order goes up, bond length goes down

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## Principle #4 of MO Theory

**Principle #4:**

Atomic orbitals combine to give molecular orbitals **only** when the atomic orbitals are of **similar energy**

**Similar energy = better overlap**

- 1s + 1s = good MO
- 1s + 2s = poor MO
- 2s + 2s = good MO
- 2s + 2p = poor MO
- 3s + 2s = poor MO
- ... etc. ...

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## MO Diagram for Dilithium, Li<sub>2</sub>

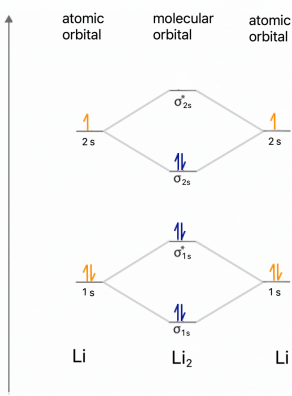
Note: no overlap between 1s and 2s

$$\text{Bond Order} = \frac{1}{2} (4 - 2) = 1$$

**Stable molecule**

*Would you expect Be<sub>2</sub> to exist? Why?*

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## 2p orbitals, $\sigma$ and $\pi$ bonds

Three possible p orbitals on each atom - **six total** p MO orbitals

Two p orbitals create **2  $\sigma$  MO bonds**

Four remaining p orbitals create **4  $\pi$  MO bonds**

Four p atomic orbitals create four  $\pi$  molecular orbitals,

$\pi$  = bonding (2)

$\pi^*$  = antibonding (2)

*... but there's a catch!*

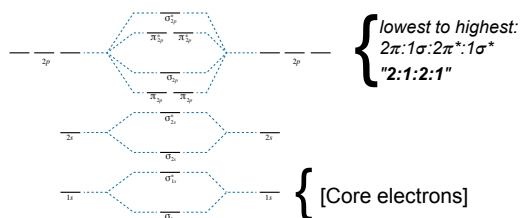
MAR

## 2p orbitals, $\sigma$ and $\pi$ bonds for "NBC"

For **B**, **C** and **N** ("NBC"),

$\pi$  orbitals lower energy than  $\sigma$  orbital

$\pi^*$  orbitals lower energy than  $\sigma^*$  orbital



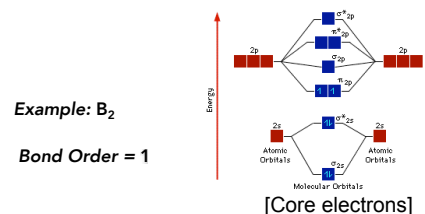
MAR See MO Diagram ( $B_2 - N_2$ ) Handout

## 2p orbitals, $\sigma$ and $\pi$ bonds for "NBC"

For **B**, **C** and **N** ("NBC"),

$\pi$  orbitals lower energy than  $\sigma$  orbital

$\pi^*$  orbitals lower energy than  $\sigma^*$  orbital



Example:  $B_2$

Bond Order = 1

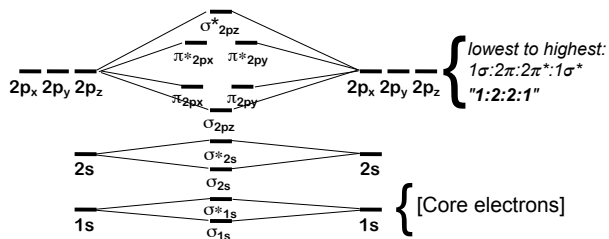
MAR See MO Diagram ( $B_2 - N_2$ ) Handout

## 2p orbitals, $\sigma$ and $\pi$ bonds for "FONe"

For **F**, **O** and **Ne** ("FONe"),

$\sigma$  orbital lower energy than  $\pi$  orbitals

$\pi^*$  orbitals lower energy than  $\sigma^*$  orbital



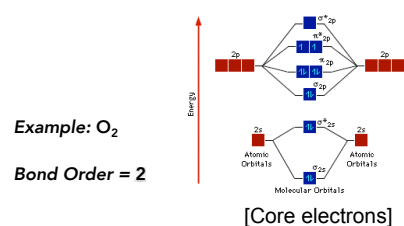
MAR See MO Diagram ( $O_2 - Ne_2$ ) Handout

## 2p orbitals, $\sigma$ and $\pi$ bonds for "FONe"

For **F**, **O** and **Ne** ("FONe"),

$\sigma$  orbital lower energy than  $\pi$  orbitals

$\pi^*$  orbitals lower energy than  $\sigma^*$  orbital



Example:  $O_2$

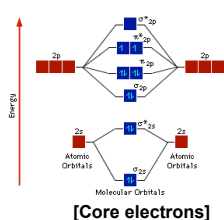
Bond Order = 2

MAR See MO Diagram ( $O_2 - Ne_2$ ) Handout

## Paramagnetism

Paramagnetism exists when unpaired electrons found in MO diagram

$O_2$  is paramagnetic;  
 unpaired electrons  
 in two  $\pi^*$  orbitals

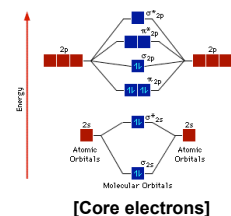


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## Paramagnetism

Paramagnetism exists when unpaired electrons found in MO diagram

$N_2$  is diamagnetic;  
 all electrons paired



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## Ionic Diatomic Molecules

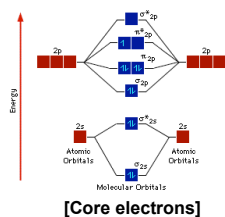
Predicting Ionic Diatomic MO diagrams simple: start with neutral molecule, then add or subtract electrons as necessary

Use Hund's rule and Pauli exclusion principle; re-check magnetism, bond order, etc.

**Example:  $O_2^{1+}$**

Remove electron from  $\pi^*_{2p}$  orbital

bond order = 2.5,  
paramagnetic



Electrons are removed from the Highest Occupied Molecular Orbital (HOMO) in the molecule

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## Ionic Diatomic Molecules

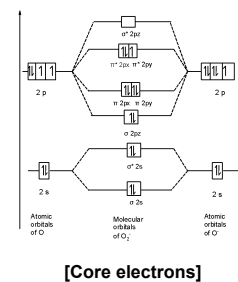
Predicting Ionic Diatomic MO diagrams simple: start with neutral molecule, then add or subtract electrons as necessary

Use Hund's rule and Pauli exclusion principle; re-check magnetism, bond order, etc.

**Example:  $O_2^{1-}$**

Add electron to  $\pi^*_{2p}$  orbital

bond order = 1.5,  
paramagnetic

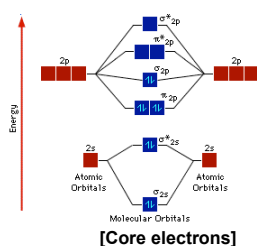


Electrons are added from the Lowest Unoccupied Molecular Orbital (LUMO) in the molecule

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## Molecular Orbital Shorthand Notation

Used to abbreviate the MO diagrams



- Ignore core electrons (all 1s interactions only) by writing **[core electrons]**
- combine  $\pi_{2px}$  and  $\pi_{2py}$  into one  $\pi_{2p}$  parentheses (same with antibonding)
- Write in order of **increasing energy**

For  $N_2$ :

**[core electrons]( $\sigma_{2s}$ )<sup>2</sup>( $\sigma^*_{2s}$ )<sup>2</sup>( $\pi_{2p}$ )<sup>4</sup>( $\sigma_{2p}$ )<sup>2</sup>**

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## Sigma and Pi Bonds

Determine sigma and pi bonds using:

$$\# \sigma \text{ bonds} = \frac{1}{2} (\# \sigma \text{ bonding e}^- - \# \sigma \text{ antibonding e}^-)$$

$$\# \pi \text{ bonds} = \frac{1}{2} (\# \pi \text{ bonding e}^- - \# \pi \text{ antibonding e}^-)$$

and

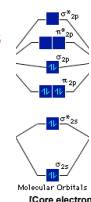
$$\text{bond order} = \# \sigma \text{ bonds} + \# \pi \text{ bonds}$$

For  $N_2$ : **[core electrons]( $\sigma_{2s}$ )<sup>2</sup>( $\sigma^*_{2s}$ )<sup>2</sup>( $\pi_{2p}$ )<sup>4</sup>( $\sigma_{2p}$ )<sup>2</sup>**

$$\# \sigma \text{ bonds} = \frac{1}{2}(4 - 2) = 1 \sigma \text{ bond}$$

$$\# \pi \text{ bonds} = \frac{1}{2}(4 - 0) = 2 \pi \text{ bonds}$$

$$\text{bond order} = \frac{1}{2}(8 - 2) = 3 = 1 \sigma + 2 \pi \text{ bonds}$$



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## MO Diagram for Diatomics

	Large 2s-2p interaction			Small 2s-2p interaction		
	B <sub>2</sub>	C <sub>2</sub>	N <sub>2</sub>	O <sub>2</sub>	F <sub>2</sub>	Ne <sub>2</sub>
$\sigma^*_{2p}$						
$\pi^*_{2p}$						
$\sigma_{2p}$						
$\pi_{2p}$						
$\sigma^*_{2s}$						
$\sigma_{2s}$						
Bond order	1	2	3	2	1	0
Bond enthalpy (kJ/mol)	298	620	941	495	155	—
Bond length (Å)	1.59	1.31	1.10	1.21	1.43	—
Magnetic behavior	Paramagnetic	Diamagnetic	Diamagnetic	Paramagnetic	Diamagnetic	—

Note: all should have [core electrons]

Changes in MO diagrams due to  
s-p mixing and/or electron repulsion

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## MO Application: Vision

Molecular Orbital Theory helps to describe the process of vision -  
**photochemistry**



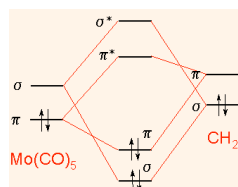
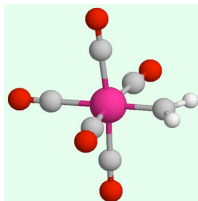


## End of Chapter 5

See:

- Chapter Five Study Guide
- Chapter Five Concept Guide
- Important Equations (following this slide)
- End of Chapter Problems (following this slide)

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MO Diagram for Mo(CO)<sub>5</sub>=CH<sub>2</sub>

## Important Equations, Constants, and Handouts from this Chapter:

- the bond order, bond energy and bond length relationships
- know the advantages and disadvantages of the Valence Bond and Molecular Orbital theories
- see the **Geometry and Polarity Guide** and the two **Molecular Orbital Theory** diagrams (NBC and FONE) (handouts)

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**Valence Bond / Hybridization Theory:** types of hybridization (sp, sp<sup>2</sup>, etc.), sigma and pi bonds

**Molecular Orbital Theory:** bonding and antibonding orbitals, sigma bonds and pi bonds, paramagnetic and diamagnetic, the "NBC" vs. "FONE" diagrams

$$\text{bond order (MO theory)} = \frac{1}{2}(\# \text{ bonding } e^- - \# \text{ antibonding } e^-)$$

## End of Chapter Problems: Test Yourself

- Specify the electron-pair and molecular geometry for each of the following. Describe the hybrid orbital set used by the central atom in each molecule or ion.  
a. BBr<sub>3</sub> b. CO<sub>2</sub> c. CH<sub>2</sub>Cl<sub>2</sub> d. XeF<sub>4</sub>
- Use MO theory to tell which has the largest bond order: C<sub>2</sub> or F<sub>2</sub>. Are either species paramagnetic?
- Use MO theory to speculate on the existence of dilithium.
- Which compound is stronger by MO theory: Be<sub>2</sub> or B<sub>2</sub><sup>+</sup>?
- Describe the hybridization change on carbon as methane (CH<sub>4</sub>) is burned to create carbon dioxide.

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## End of Chapter Problems: Answers

- a. trigonal planar, trigonal planar, sp<sup>2</sup>. b. linear, linear, sp. c. tetrahedral, tetrahedral, sp<sup>3</sup>. d. octahedral, square planar, sp<sup>3</sup>d<sup>2</sup>
- BO(C<sub>2</sub>) = 2, diamagnetic. BO(F<sub>2</sub>) = 1, diamagnetic.
- By MO theory, dilithium (Li<sub>2</sub>) should exist (BO = 1, diamagnetic.)
- MO theory would predict that B<sub>2</sub><sup>+</sup> (bond order = 0.5, paramagnetic) is stronger than Be<sub>2</sub> (bond order = 0, this should not exist at all.)
- sp<sup>3</sup> to sp

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